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Course Name: Physics
Unit Title: Buoyancy

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Grade Level: HS Juniors and Seniors
Concept: Factors affecting buoyancy

Goal: The goal of this combination lesson-lab is to get students to use inquiry to learn how various factors determine the force of buoyancy.

Objectives: At the conclusion of this exercise the students will demonstrate the ability to:

1. state which of a number of factors affect buoyancy, and which do not.
2. use scientific instruments to determine the relationships between buoyancy and pertinent factors such as triple-beam balance, graduated beakers, pulleys, and computers.
3. state the nature of the relationship between the various pertinent factors and buoyancy.
4. derive the algebraic relationship between buoyancy and other pertinent factors.
5. work numeric problems using the derived relationship.
6. explain how the algebraic relationship was derived.
7. use basic formulae to calculate volumes of different standard forms (sphere, cylinder, etc.)
8. explain the basic nature of scientific research using buoyancy as an example.

## Content:

I. Buoyancy is affected by the following parameters of the system --
A. Volume of object immersed
B. Density of immersing liquid
C. Acceleration due to gravity
II. Buoyancy is not affected by the following parameters of the object immersed -
A. Depth of immersion
B. Composition
C. Density
D. Depth
E. Weight
F. Shape
G. Mass
III. Mathematical relationships exists between buoyancy and pertinent factors:
A. Buoyancy is proportional to volume of the object immersed
B. Buoyancy is proportional to the density of the liquid in which the object is immersed
C. Buoyancy is proportional to the ambient acceleration due to gravity

Lesson Overview: Students will predict which factors affect buoyancy. They will then design ways to test these predictions given a number of experimental items.

Lab Overview: Once the factors that affect buoyancy are identified, students will design and carry out a controlled scientific study to determine the relationships between buoyancy and these various factors.

Procedure: Because this is an inquiry lesson, questions will guide the discussion throughout. Students will direct the discussion and class activities by their responses to questions and suggestions for experiments. Here are the basic questions that will be followed throughout the lesson.

Day 1 (Inquiry Lesson):

STATE LEARNING GOAL - The objective behind the next two class periods is to find the mathematical relationship between buoyancy and the factors that affect it.

## TALKING POINTS

Q. How do you measure the buoyant force experienced by an object submerged in a liquid?

Note: Place weight on spring balance into water.
Q. What is being measured this time?
Q. Have you noticed that there is a difference in air \& submerged weight? Why?
Q. How can we calculate the buoyant force of the liquid?

Note: $\mathrm{Fb}_{\mathrm{b}}=\mathrm{W}_{\mathrm{a}}-\mathrm{W}_{\mathrm{l}}$
Q. If this weight is submerged only partially in the liquid, how can we measure and calculate the buoyant force exerted on it?

Note: Observe that the smaller the submersion, the smaller the buoyant force.
Note: Float wood on surface of water.
Q. What is the buoyant force exerted on the wood by the water?

Note: Slowly immerse the wood on a scale into the water. Give the weight until 0 .
Q. Do you understand why the scale reads zero?

Note: $\mathrm{W}_{\mathrm{a}}=\mathrm{F}_{\mathrm{b}} \quad\left(\mathrm{F}_{\mathrm{b}}=\mathrm{W}_{\mathrm{a}}-0\right)$
Q. What physical factors might affect the buoyant force exerted on a body?

Note: possible factors: density of liquid, orientation, depth, weight or composition, orientation, shape, volume or size, etc.
Q. Is the buoyant force experienced by a submerged object related to its shape?

Note: Test with a clay bob, deforming after first test.
Q. Does the buoyant force experience by a submerged object depend on its orientation?

Note: Test with a block of aluminum oriented along three different axes.
Q. Is the buoyant force experienced by a submerged object related to its size?

Note: Test using two different sized objects of same weight (plexi cyl \& 100 g weight).
Q. Is the buoyant force exerted on a body dependent upon the weight of a body?

Note: Test with aluminum and copper ingots of identical volume.
Q. From what you've seen thus far, can you tell me if the buoyant force depends upon the density of a body?
Q. Is the buoyant force exerted by a liquid dependent upon the depth?

Note: Check buoyant force at varying depths.
Q. Is the buoyant force exerted by a liquid dependent upon the type of liquid?

Note: Test using fresh and then salt water.
Day 2 (Jigsaw version of Bounded Lab - one group finds relationship between buoyancy and density of liquid and other groups find relationship between buoyancy volume of object):

Summary of findings thus far --
$\mathrm{Fb}_{\mathrm{b}}$ depends upon:
density of liquid
volume of object
$\mathrm{Fb}_{\mathrm{b}}$ DOES NOT depend upon:
density of object
depth of object
shape of object
weight of object
mass of object
Working relationships:

$$
\begin{gathered}
\mathrm{F}_{\mathrm{b}}=\mathrm{W}_{\mathrm{a}}-\mathrm{W}_{l} \\
\mathrm{~F}_{\mathrm{b}}=\mathrm{W}_{\mathrm{a}} \text { (floating) }
\end{gathered}
$$

Q. How does the buoyant force depend upon the volume of the object?
Q. How does the buoyant force depend upon the density of the liquid?

Note: Students design and perform experiments to find proportionalities between $\mathrm{Fb}_{\mathrm{b}}, \mathrm{V}_{\mathrm{o}}$, and $\rho_{\ell}$. Note: Hypothesize relationship between all variables:

$$
\begin{gathered}
\mathrm{a} \rho_{l}+\mathrm{b}=\mathrm{c} \mathrm{~V}_{\mathrm{O}}+\mathrm{d} \\
\mathrm{Fb}=\mathrm{a} \rho_{\ell} \mathrm{V}_{\mathrm{O}}+\mathrm{\sigma} ? \\
\mathrm{Fb}_{\mathrm{b}}=\mathrm{a} \rho_{\ell}+\mathrm{cV}_{\mathrm{o}}+\mathrm{e} \quad ?
\end{gathered}
$$

Note: Students find, give, and explain actual mathematical relationship.

## Assessment: Follow-up Questions \& Problems

Q. Which of the above represents the true relationship between variables?
Q. Why do objects experience an buoyant force?
Q. Will objects lying on the bottom of a fluid experience a buoyant force?
Q. Is it true that light objects float while heavy objects sink? (penny versus a block of wood)
Q. What conditions of density determine whether or not an object will float in a fluid?
Q. How can you measure the buoyant force when a piece of wood is completely submerged in water?
Q. How much buoyant force is exerted on a 14 -inch diameter basketball immersed in pure water?
Q. You are on an unnamed planet and you want to find the acceleration due to gravity. A 3-cm diameter aluminum ball immersed in pure liquid water experiences a buoyant force of 0.15 newtons. What is the acceleration due to gravity?
Q. An object with a volume of $10 \mathrm{~cm}^{3}$ experiences a force of 0.5 newtons on the surface of the earth. What is the density of the fluid?

## Materials:

| Triple-beam balance | String | Beakers |
| :--- | :--- | :--- |
| Pyknometer | Vernier caliper Clay | Alcohol |
| Computer w/ Graph Analysis | Beakers |  |
| Volume formulae for regular |  |  |
| polygons | Miscellaneous objects with <br> different densities and <br> shapes | Olive oil <br> Water and Salt <br> Honey <br> Hydrometer |

A good follow-up activity deals with hypothetical inquiry. What is the source of the buoyant force? The teacher can demonstrate increasing pressure with depth by using a 2 or 3 -liter soda bottle with holes drilled into the side. The water at the lowest level will shoot out farthest, the water at the highest level will show out the least far. This is because of pressure differences.

If pressure is merely due to the weight of the water, then $p=\rho g d$ where d is the depth. By looking at the difference of pressure per unit area at two depths, one can derive from this consideration alone the resulting formulation $F_{b}=\rho V g$

